



RESEARCH METHODS
for science

MICHAEL P. MARDER

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RESEARCH METHODS FOR SCIENCE

A unique introduction to the design, analysis, and presentation of scientific projects, this is an essential textbook for undergraduate majors in science and mathematics.

The textbook gives an overview of the main methods used in scientific research, including hypothesis testing, the measurement of functional relationships, and observational research. It describes important features of experimental design, such as the control of errors, instrument calibration, data analysis, laboratory safety, and the treatment of human subjects. Important concepts in statistics are discussed, focusing on standard error, the meaning of p -values, and the use of elementary statistical tests. The textbook introduces some of the main ideas in mathematical modeling, including order-of-magnitude analysis, function fitting, Fourier transforms, recursion relations, and difference approximations to differential equations. It also provides guidelines on accessing scientific literature, and preparing scientific papers and presentations. An extensive instructor's manual containing sample lessons and student papers is available at www.cambridge.org/Marder.

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Research Methods for Science

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Preface

This book accompanies a one-semester undergraduate introduction to scientific research. The course was first developed at The University of Texas at Austin for students preparing to become science and mathematics teachers, and has since grown to include a broad range of undergraduates who want an introduction to research. The heart of the course is a set of scientific inquiries that each student develops independently. In years of teaching the course, the instructors have heard many questions that students naturally ask as they gather data, develop models, and interpret them. This book contains answers to those most common questions.

Because the focus is on supporting student inquiries, the text is relatively brief, and focuses on concepts such as the meaning of standard error, p -values, and deterministic modeling. If a single statistical test, such as χ^2 , is adequate to deal with most student experiments, the text does not introduce alternatives, such as ANOVA, even if they are standard for professional researchers to know.

The mathematical level of the book is intermediate, and in some places presumes knowledge of calculus. It could probably be used with students who don't know calculus, skipping these sections without great loss.

There is an instructor's manual that describes daily activities for a 14-week class that meets two hours per week in a classroom and two hours per week in a lab. It is available at www.cambridge.org/Marder. The classroom sessions are not lectures covering the material in these chapters, but instead consist in activities focusing on basic concepts. The text in many cases contains more complete explanation than there is time to deliver in class.

The basic idea for the class and hence of this book is due to David Laude, Professor of Chemistry and Associate Dean for Undergraduate Education at UT Austin. He had two essential insights: First, the way to learn about scientific research is actually to do some. Second, it doesn't matter if research results are not new so long as they are new to the person who does them. The ingenious order

“BE CURIOUS!!” in the first inquiry assignment (page 15) comes from his first assignment in the first semester he taught it.

Many other course instructors have contributed. Mary Walker and Denise Ekberg both brought in course elements because of their backgrounds that span scientific research and secondary teaching. They emphasized the importance of procedures to ensure student safety, and also insisted on rubrics and checklists so that students received clear messages during an otherwise free-wheeling class of what was acceptable, what was forbidden, what was desired, and what was discouraged. Thomas Hills emphasized the importance of open questions. Many teaching assistants have also contributed to the course content, particularly Sed Keller, who wrote the first draft of the appendix on use of spreadsheets.

For many years, I have co-taught the class with Pawan Kumar, Professor of Astronomy, and Dan Bolnick, Associate Professor of Integrative Biology. Pawan Kumar helped create all the homeworks, and insisted we find ways to tie research on closed questions back into research on areas of social concern. Dan Bolnick gently prodded me to throw out all previous approaches to statistics, and make use of examples from biology that worked much better.

Finally, I would like to thank Mary Ann Rankin, Dean of the College of Natural Sciences, who insisted passionately from the start that future teachers in our UTeach program learn about scientific research, and has provided every form of support needed to help the class grow.

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1

Curiosity and research

1.1 Course goals

Science starts with curiosity about the world. It starts with questions about why the sky is blue, why dogs wag their tails, whether electric power lines cause cancer, and whether God plays dice with the universe. But while curiosity is necessary for science, it is not enough. Science also depends upon logical thought, carefully planned experiments, mathematical and computer models, specialized instruments, and many other elements. In this course, you will learn some of the research methods that turn curiosity into science. In particular, you will learn to

- Create your own experiments to answer scientific questions.
- Design experiments to reduce systematic and random errors and use statistics to interpret the results.
- Use probes and computers to gather and analyze data.
- Treat human subjects in an ethical fashion.
- Apply safe laboratory procedures.
- Find and read articles in the scientific literature.
- Create mathematical models of scientific phenomena.
- Apply scientific arguments in matters of social importance.
- Write scientific papers.
- Review scientific papers.
- Give oral presentations of scientific work.

You will not just be learning about these skills. You will be acquiring and applying them by carrying out scientific inquiries.

1.2 Kinds of questions

Testable questions Every scientific inquiry answers questions, and most scientific inquiries begin with specific questions. People often wonder about questions that are hard to address, such as

- Why is the sky blue?
- What are stars and why do they move at night?
- What is sound?
- Why are leaves green?
- How do you grow the biggest possible tomatoes?
- Why do balloons pop?
- How can you cure a cold?
- Why is lighter fluid bad to drink?

Questions that begin with “Why,” “What,” or “How” often ask for an explanation of something that is very complex, and give little guidance about how to begin finding an answer. *Testable questions* on the other hand suggest specific activities that may provide an answer. Some examples:

- Is the sky more blue on a clear day in summer than on a clear day in winter? [Take digital photographs of the sky at noon on many days during the summer and many days during the winter with the same camera, using the same f-stop and shutter speed, and at the same location, recording temperature, humidity, and cloud cover. Compare the numerical values of the pixels in the two sets of photographs.]
- Are there chemical solvents that remove from a leaf the substances that make it green? [Grind up leaves in solvents such as water, acetone, and alcohol and check whether the green color can be extracted.]
- How does the loudness of a balloon popping depend on how much one blows it up? [Blow up balloons to different diameters and pop them at a fixed distance from a microphone connected to a digital sound recording device.]
- Is lighter fluid poisonous for ants? [Spray a mist of lighter fluid on ants, and compare their behavior with ants not sprayed with lighter fluid.]

Most of this class will be devoted to building experiments and carrying out analyses to answer testable questions. Sometimes the answers to the questions are known and one could look them up. In fact, part of the course will deal with techniques for looking up known answers. But the point of this class is not so much to answer particular questions as to provide experience in how scientists answer questions.

Closed and open questions Another way to categorize questions is to divide them between closed and open. *Closed questions* are those with a specific answer that is already known. Some examples:

- What is the name of the third planet from the Sun?
- What is the indefinite integral of $\tan \theta$ with respect to θ ?
- At what rate does a ball accelerate when dropped near the surface of the Earth?
- What is the pH of an orange?
- How many vertebrae are there in the spine of a rhesus monkey?
- How large are the largest tides observed in the Bay of Fundy?

Open questions may have multiple answers, and require much more thought and interpretation. Some examples:

- How did the third planet from the Sun get there?
- Is the unproved conjecture “Every even integer greater than 2 can be represented as the sum of two primes” provable or unprovable?
- Are the fundamental constants of physics changing over time?
- Is it possible to make a completely synthetic juice that tastes as good and is as healthy as orange juice?
- Are there mutations of the rhesus monkey that are immune to any form of common cold?
- How much will the mean sea level change over the next 100 years?

Closed questions are not very challenging if someone just gives you the answer, but they can be demanding indeed if you are the one responsible for finding it. Making progress on open questions often involves answering a series of closed questions. For example, making predictions about the mean sea level over the next 100 years should be influenced by careful measurements of the mean sea level today. Checking whether the constants of nature are changing requires measuring very carefully their current values. Learning how the Earth came to its current orbit around the Sun is aided by knowing the the mass and chemical composition of the Sun and the Earth.

So, while most scientists have open questions in the backs of their minds while they work, and are motivated by large and significant issues, they spend most of their time taking small steps, answering closed questions. You should not worry if your first steps in science address apparently simple questions. Learn the process by which scientists solve simple problems well, and you will have gained skills to begin addressing the largest questions of the day.

1.3 Research methods for science

Scientists spend their time in many ways, and using a wide variety of research methods. The following sections describe some of the most common. They are based upon practical observation of how scientists spend their time and the sorts of investigations described in published papers and in conference presentations.

1.3.1 Test a hypothesis: Hypothesis-driven research

One research method in particular is usually singled out by introductory science texts and called *the Scientific Method*. Steps in this method are

1. State a hypothesis.
2. Design an experimental procedure to test the hypothesis.

3. Construct any necessary apparatus.
4. Perform the experiments.
5. Analyze the data from the experiment to determine how likely it is the hypothesis can be disproved.
6. Refine or correct the hypothesis and continue if necessary.

Hypothesis-driven research begins (no surprise) with a hypothesis. A *hypothesis* is a statement about the world that can be true or false, and whose truth is being tested. A valid hypothesis must be *falsifiable* (Popper, 1959). This means you should imagine actually being able to show it to be false, and you should be able to imagine evidence that would make enthusiastic supporters of the hypothesis abandon it. For example, the hypothesis that people cannot cause spoons to float in the air using mental energy could be falsified by finding a single person reproducibly capable of making spoons float without the aid of wires or other supports. When a hypothesis is *valid*, it meets the rules for being a hypothesis, whether it is true or false, while if a hypothesis is invalid it breaks the rules and should not be considered. Table 1.1 provides examples of valid and invalid hypotheses.

The U.S. National Institutes of Health, which funds most of the basic medical research in the United States, divides research into two categories: hypothesis-driven research and curiosity-driven research. The National Institutes of Health almost exclusively funds hypothesis-driven research. Both hypothesis-driven and curiosity-driven research have their place, and science needs both of them to function.

Hypothesis-driven research is most appropriate when a researcher is trying to decide between a small number of mutually exclusive cases, such as finding which of two medical treatments is more effective, or whether electric power lines cause cancer. Hypothesis testing is particularly important in medical research, since nothing is more likely to cause people to invest in ineffective procedures or drugs than hopes of a cure for themselves or loved ones. Hypothesis-driven research is designed to protect researchers against subtle biases that can distort research outcomes and are particularly difficult to avoid when life and health are at stake. Biases are also hard to avoid whenever any participants in the research have preconceived notions of what the results should be. Procedures to avoid bias in hypothesis-driven research are described in more detail in Chapter 2.

Hypothesis-driven research is not appropriate when the researcher is trying to decide between a vast number of possible cases. For example, suppose one is given a rock and wants to know its density. There is nothing to stop the researcher from beginning the investigation by saying “My hypothesis is that the density of this rock is 1 gm/cm^3 ” and testing the hypothesis. Starting an inquiry with a rough estimate of what the answer should be expected to be is always a good idea. However, calling

Table 1.1 Various statements that could be considered as scientific hypotheses with comments on whether they are valid or not.

Statements	Comments
Briar's Aspirin cures headaches faster than RCS Aspirin.	Valid hypothesis. Can be checked by using the two forms of aspirin on randomly chosen populations of headache sufferers.
Eating two ounces of olive oil a day decreases the odds of contracting heart disease.	Valid hypothesis. Can be checked by randomly assigning large numbers of people diets that contain or do not contain two ounces of olive oil and monitoring their health over long periods of time.
The gravitational force between two masses is proportional to the products of the masses and decreases exponentially with the distance between the masses.	Valid hypothesis. Also false, since gravitational force decreases as the square of the distance, not as the exponential.
If electrons were 10% less massive, no life would exist in the universe.	Fascinating statement, but not a valid and testable hypothesis, particularly since it is impossible to anticipate all forms that life could take.
A Toyota Camry weighs exactly 1000 kg.	This is a valid hypothesis, but it is silly if left as a hypothesis. There is no reason that the weight of a car should come out to be such a neat round number.
What is the best fertilizer to use to get large and tasty tomatoes?	Not a valid hypothesis. Hypotheses have to be definite statements, and cannot be questions.
Macs are better than PCs.	Not a valid hypothesis. It is impossible to imagine evidence that could sway the enthusiastic supporters of each kind of computer to accept the other as better.

the estimate a hypothesis is not helpful, because hypotheses are supposed to be tested rigorously and rejected if they do not meet high standards of evidence. The density of a rock can have a continuous range of values. Even if the answer must lie somewhere between 0.1 gm/cm^3 and 10 gm/cm^3 there is an infinite number of possibilities. Thus by picking a single value at the outset of the investigation and testing it, the odds are overwhelming that the hypothesis will be rejected. The problem is that it is very unlikely that anyone cares particularly whether the density of the rock is exactly 1.0 gm/cm^3 or not, and if someone were to say "I have tested the hypothesis that this rock has a density of 1.0 gm/cm^3 and rejected it" the natural response would be "Please, just tell me the density of the rock." This comment leads to other modes of research.

1.3.2 Measure a value: Experimental research (I)

1. Identify a well-defined quantity.
2. Design a procedure to measure it.
3. Perform the experiments.
4. Analyze and report on the accuracy of the results.

Measuring a single number well is often much harder than it seems, and some of the technical issues involved are discussed in more detail in Section 2.2. Examples of measured quantities, ranging from fairly simple to very challenging, appear in Table 1.2. Some of the primary challenges in measuring values have to do with errors in the measurement process. *Random errors* reveal themselves because of continual variations in the values one obtains with repeated measurement. *Systematic errors* are more difficult to catch because the same error occurs at the same size in every measurement, and such errors can only be eliminated either by thinking through the sources of problems and removing them, or by finding completely independent ways to make the measurements and comparing them.

Measuring a few numbers underlies many of the most expensive large group projects in science. Experimental particle physics, which employs thousands of scientists at international laboratories with budgets in the hundreds of millions of dollars, is devoted to finding masses and charges of a small number of elementary particles. The Human Genome Project (GENOME, 2008) was one of the great triumphs of science in the last 50 years, yet it consisted at a primitive level in finding a long sequence composed of four letters, which one can think of as a single very large number in base 4. Government agencies like to fund projects of this type for the simple reason that the success of the project is almost guaranteed. The researchers will come up with a collection of numbers, and those numbers are a deliverable that the government agency can display to show that the money was well spent.

Measuring a single value is often the starting point for testing a hypothesis or measuring a series of related values. Therefore even when a single number is not the primary aim of a research project, being able to measure numbers is a basic skill that underlies all modes of research.

1.3.3 Measure a function or relationship: Experimental research (II)

1. Observe a phenomenon and develop testable questions.
2. Identify control variables and response functions.
3. Design an experimental procedure to vary the control variables, measure the response variables, and keep other factors constant.

Table 1.2 Examples of values that scientific researchers might be interested in measuring.

Value	Comments
Density of crystalline silicon at room temperature	Density cannot be obtained directly, but is defined to be the ratio of mass to volume, and so can be obtained by separately measuring mass and volume of crystalline samples and taking the ratio.
Charge of the electron	The first experimental information obtained at the end of the nineteenth century about the electron was the ratio of charge to mass. The physicist Robert Millikan won a Nobel Prize for a series of experiments between 1910 and 1920 involving oil droplets that made it possible to determine the charge separately.
Mass of the electron neutrino	The electron neutrino is one of the most plentiful particles in the universe, but it reacts very rarely with ordinary matter and is therefore almost invisible to us. All experiments to determine its mass have so far concluded that it was too small to measure, but even a very slight mass has great implications for the total amount of matter in the universe. One current experiment to measure the electron neutrino mass is being conducted at the Research Center of Karlsruhe in Germany and has a budget of 33 million euros (KATRIN, 2008).
Distance from Earth to the nearest star other than the Sun.	Proxima Centauri is 4.22 light years or 39,900,000,000,000 km from Earth (NASA, 2008).
The number of base pairs and distinct genes in the human genome	The number of base pairs is around 3 billion and the number of distinct genes is around 30,000. These values were determined as part of the Human Genome Project (GENOME, 2008), a multibillion dollar scientific effort that involved government and university scientists, as well as a corporation, and provided the first sequencing of the human genome.

4. Perform the experiments.
5. Analyze the relation between control variables and response variables, and characterize the relation mathematically.

Much of experimental physics and chemistry operates according to this research method; examples appear in Table 1.3. The starting point is to identify *control variables* and *response variables*. A control variable is a quantity that the experimenter varies at will to change the character of the experiment, while a response

Table 1.3 Examples of functions or relationships that researchers might measure.

Function or relationship	Comments
Find how the speed of sound in air at fixed pressure depends upon air temperature.	The control variable is temperature, and the response variable is sound speed. This sort of experiment is extremely common in experimental physics and chemistry, and reference volumes are full of the results. Examples are provided by the hundreds of volumes called <i>Numerical Data and Functional Relationships in Science and Technology</i> by Landolt and Börnstein, published in multiple series over many decades by Springer-Verlag, originally in German, and now in English.
Place a fluid between two cylinders, rotate the outer cylinder, and find the state of the fluid as a function of the rotation speed.	The control variable is rotation speed of the cylinder. The fluid undergoes a number of abrupt qualitative transitions, from smooth uniform motion, to rolls that look like a barber pole, to turbulence.
Measure the stiffness of a sample of rubber as a function of the amount of cross-linking agent used to process it.	The control variable is cross-linking agent (Charles Goodyear used sulfur to stiffen natural rubber) and the response variable is stiffness. This type of measurement is commonplace in engineering and industrial research.
Find the average size of a specific breed of tomatoes grown in specific soil and climate as a function of the amount of salt in the soil.	The control variable is salt concentration, and the response variable is tomato size. An experiment like this that really sought to optimize the size of tomatoes would not typically focus on a single variable. Instead a series of factors such as salt concentration, fertilizer, irrigation, and seed type would all become part of an experimental design to improve tomatoes.
Measure how often allergy sufferers sneeze per day as a function of the dose of anti-histamine they take.	The control variable is the dose of anti-histamine. Different allergy sufferers are sensitive to different substances, all of which are likely to be varying beyond control of the experimenter.

variable is some other quantity measured as an outcome. In a good experiment, all variables other than the control variables that affect the outcome are held constant. So in measurements of the speed of sound in air with respect to temperature, the pressure and humidity of air need to be kept constant. In measuring the stiffness of rubber with respect to a cross-linking agent, the temperature needs to be held constant. An experiment on the effectiveness of an anti-histamine to prevent sneezing would raise the greatest challenges of this sort, since one person might be allergic to cats, another to mold in the air, and it would be difficult either to find lots of subjects all allergic to exactly the same thing or to control the precise amount to which they were exposed.

There are many different skills involved in actually carrying out experiments, ranging from construction of apparatus and safe laboratory practice to the safe and ethical treatment of human subjects. These and other technical issues are discussed at greater length in Chapter 2.

The mathematical analysis of a largely experimental project may involve nothing more than careful characterization of error bounds associated with each measured point. Or it may involve careful comparison with a particular mathematical theory of the experiment. Sometimes the analysis involves actual construction of a mathematical model, as in the next method of research.

1.3.4 Construct a model: Theoretical sciences and applied mathematics

1. Choose a relationship discovered through experimental investigation.
2. Construct mental pictures to explain the relationship, and develop hypotheses about origins of the phenomenon.
3. Identify basic mathematical equations from which the relation might result.
4. Using analytical or numerical techniques, determine whether the experimental relationship results from the basic mathematical equations.
5. If incorrect, find a new mathematical starting point.
6. If correct, predict new relationships to be found in future experiments.

This mode of research describes much of applied mathematics, theoretical physics, theoretical chemistry, theoretical geology, theoretical astronomy, or theoretical biology (Table 1.4). For example, the experimental observation might be intense bursts of gamma-rays. A hypothesis might be that they emerge from gravitational collapse of certain stars. A lengthy process of modeling the collapse of stars, trying to calculate the radiation that emerges from them, would be needed to check the hypothesis.

In variants of this mode of research, the modeling takes place without any experimental input, and emerges with experimental predictions. In other variants, this type of research can lead to new results in pure mathematics.

1.3.5 Observational and exploratory research

1. Create an instrument or method for making observations that have not been made before.
2. Carry out observations, recording as much detail as possible, searching for unexpected objects or relationships.
3. Present results and stimulate further research.

Laboratory experiments have control variables, but in a huge variety of scientific investigations, scientists measure quantities they cannot control. This mode

Table 1.4 Examples of models of scientific phenomena.

Model	Comments
Calculate the distance a projectile fired from a barrel near the Earth's surface at known speed will travel as a function of angle.	The calculation can be performed using Newton's laws of motion. It is fairly easy if one neglects things such as air resistance and the Earth's rotation, and more challenging if these are included.
Consider a fluid placed between two cylinders with the outer one rotating and calculate the rotation speed at which steady fluid motion becomes unstable to the formation of rolls.	This computation was first carried out by Taylor (1923) using equations for fluids called the Navier–Stokes equations, and constituted the first nontrivial comparison of theory and experiment for fluid motion.
Find the arrangement of atoms in deoxyribonucleic acid (DNA).	Watson and Crick (1953) determined the structure of DNA. Although their article contains a few numerical values, the paper mainly contains the concept of DNA as a double helix with a schematic diagram, no complicated calculations.
Find the weather in the United States two days from now.	Weather prediction is one of the most computer-intensive activities in the world. The process of prediction begins with a vast collection of data from weather monitoring stations around the globe and continues with computations based upon equations for the motion of air including temperature, pressure, and humidity.
Find how the populations of animals change from year to year in an environment of fixed size and limited resources.	Simple iterative equations written down in the 1970s to describe the time development of populations led to the mathematical theory of chaos.

of research covers an enormous range of possibilities. It describes the expeditions that revealed the different continents to European explorers and mapped the globe. It describes first investigations when new scientific tools are developed. It describes the increasingly accurate maps of the night sky created by new generations of telescopes, or unexpected new particles discovered in particle accelerators. It describes much geological and biological field work. More examples are in [Table 1.5](#).

Many research projects contain an exploratory phase, which produces something of interest that then becomes the subject of other research methods. For example, the first observation of gamma-ray bursts by [Klebesedal *et al.* \(1973\)](#) simply reported observations of enormously powerful far-away explosions made over several years, ruled out the possibility that they were due to known sorts of

Table 1.5 Examples of observations and explorations.

Observation	Comments
Find how the position of Mars in the sky varies over times of minutes, days, hours, and years.	Careful measurements of locations of stars go back to the beginning of recorded human history. The measurements of Tycho Brahe in the late 1500s as interpreted by Kepler played a critical role in the development of modern astronomy, physics, and mathematics.
Travel to the Galapagos islands and make careful observations about wildlife.	Charles Darwin's observations of wildlife on these islands during the second voyage of the <i>Beagle</i> , 1831–1836, particularly of finches whose beaks were adapted to different food supplies in different regions, played an important role in the thinking that eventually led to the theory of evolution.
Find the percentage of adult U.S. residents whose height lies between 30 and 31 cm, 31 and 32 cm... 100 and 101 cm ... 250 and 251 cm ...	This is a histogram or distribution function. It provides information that goes beyond simply recording average values. Many quantities, such as people's heights, are intrinsically variable, and distribution functions capture the full story.
Search for Soviet nuclear explosions in outer space.	The USSR never exploded nuclear weapons in outer space. However, the satellites the U.S. put in orbit to look for them detected massive explosions at vast distances from Earth called gamma-ray bursts.
Measure the chemical composition of Greenland ice cores as a function of depth.	Greenland ice cores provide annual information on climate and chemicals in the Earth's atmosphere going back hundreds of thousands of years. One international project was NGRIP (2003) , which obtained a 3-km-long core.
Use fMRI to map regions of activity in the brain of an individual undergoing an epileptic seizure.	Functional Magnetic Resonance Imaging (fMRI) is a tool with the ability to provide three-dimensional images of the interior of the human body, and it produces the images rapidly enough that it can even provide information on the state of the brain during specific activities.

exploding stars, and stopped. The observation triggered a long-term research effort with both theoretical and further observational components that continues to this day. The National Aeronautics and Space Administration (NASA) launched a dedicated satellite in 2004 ([SWIFT](#)) to observe gamma-ray bursts.

Many U.S. government agencies are devoted to gathering data. Even if the techniques used to assemble the data are routine and would not be called forefront

research, the methods used to gather the data are scientific. The National Institute of Standards and Technology (formerly the National Bureau of Standards) is responsible for maintaining weights and measures as required by the U.S. Constitution. Other agencies such as the Centers for Disease Control gather data about the U.S. population. Acquiring such data requires safe treatment of human subjects and methods to arrive at conclusions about a large population by sampling portions of it, techniques that will be described in Section 2.4.

1.3.6 Improve a product or process: Industrial and applied research

1. Identify market need for product.
2. Design product with the potential to meet the need.
3. Build prototype products.
4. Determine whether products function as desired.
5. Optimize products with respect to cost, speed, environmental consequences, and other factors that affect profit.
6. Bring product to market and continue.

The importance of science, scientists, and engineers in developing products has risen and fallen over the years. In the nineteenth century, national economies were based more on trades and traditional practices than on scientific methods. During the twentieth century, almost every industry and form of human activity was transformed by science and its offshoots. To mention just one example, scientific methods in farming meant that people no longer had to grow their own food, and most of the U.S. population moved to urban and suburban areas. Other examples appear in Table 1.6. Companies became so enamored of the benefits of scientific research that many established large facilities with a basic research mission. In its heyday in the 1960s, Bell Telephone Laboratories even had a composer of modern music on staff. Most of these large industrial basic research laboratories have now closed because the time interval between a basic scientific discovery and its use to make a profit is too long. Still, most companies have one or more divisions devoted to Research and Development. The research is closely tied to development of new products, and is more likely to employ people with training in engineering than in pure science. The scale of industrial research is indicated by the fact that in 2008 U.S. research and development spending was \$398 billion; the business sector spent \$268 billion, mainly on product development, while the federal government spent \$104 billion, mainly on research ([National Science Board, 2010](#)). Some industrial research is published in scientific journals, some is patented, and some is held tightly secret.

Table 1.6 Examples of products related to industrial research.

Product	Comments
Create a device to make light from electrical current.	Finding a long-lasting filament for an electric light bulb from carbonized bamboo was one of the great accomplishments of Thomas Edison's research team. A picture of a light bulb is a symbol for the idea of discovery, but real the story of the invention is complicated (Friedel and Israel, 1987). Edison ends up with credit for the bulb in part because he made it commercially successful and simultaneously created an electric power company.
Create a device from semiconducting materials capable of amplifying electrical currents.	The transistor resulted from an intensive three-year research effort at the Bell Telephone Laboratories in the late 1940s, led by William Shockley and employing John Bardeen, who is the only person ever to have won two independent Nobel Prizes in physics. This invention was the seed from which the entire electronics industry soon sprouted, and it inspired many large companies to fund basic research laboratories.
Create new small-molecule inhibitors of protein Kinase B for use as anti-cancer agents.	This example comes from a 2005 business agreement between Astra-Zeneca and a smaller firm Astex, and illustrates the very specific and goal-oriented nature of drug design. Developing a new drug involves choosing a disease whose sufferers can afford to pay for a cure, finding a cure, demonstrating its effectiveness and establishing the seriousness of side effects with extensive human trials, and marketing the drug to patients and doctors (Astra-Zeneca).
Design an airplane for trans-Atlantic flights without any wind tunnel testing.	The Boeing 777 was designed completely on computers, mainly using a program called CATIA first developed by Dassault in France (CATIA). Design on the computer made it possible to ensure that all the pieces of the airplane fit together before any of them were actually built.
Create inherently tacky elastomeric, solvent-dispersible, solvent-insoluble, acrylate copolymer microspheres.	This is the technical description of the invention that made Post-It Notes possible. It was patented in 1970 by Spencer Silver, a chemist working for 3M corporation, and after a challenging marketing campaign, because the product was initially so unfamiliar, Post-Its were distributed across the U.S. by 1980. The essential idea is to have an adhesive strong enough to hold paper, but weak enough to release the paper without tearing, and that can stick multiple times.
Write programs that regulate and control scientific instruments through computers rather than with physical knobs and switches.	Labview was first released in 1986 by National Instruments after three years of research and development. It is a complete programming language that makes it possible to control scientific instrumentation from a circuit diagram the user draws on the screen, and is now standard equipment in experimental laboratories.

1.3.7 Allied areas of research

There are many additional skills and areas of research that make scientific research possible. Here are three:

Library research *There is nothing like a few months in the lab to save a few hours in the library.* – ANON.

Because of the vast quantity of research that has already been performed, it is irresponsible to move very far through a project without attempting to determine whether the answer is already known. It is also difficult to determine with certainty whether a problem one is working on has been solved. If the problem has been solved, then the fastest way to find an answer to a scientific question is to look up the answer. Reading scientific papers can be even harder than finding them because of the specialized knowledge so often needed to make sense of them. Chapter 5 will discuss in more detail how to find results in the scientific literature, and how to read a scientific paper.

Pure mathematics *An engineer thinks that his equations are an approximation to reality. A physicist thinks reality is an approximation to his equations. A mathematician doesn't care.* – ANON.

Most of science cannot be practiced without mathematics, and much of pure and abstract mathematics was developed because of the desire to solve scientific problems. However research in pure mathematics is sufficiently different from scientific research that it is listed as an allied area rather than as part of science. Developing pure mathematics means developing conjectures about relations that might be true, defining new entities, and proving theorems. It is extraordinary that such an elaborate body of knowledge has developed from nothing but pure thought. Statements in science are accepted because they have been checked many times and (almost) always come out to be true, but mathematics has a much higher standard for truth. Mathematical statements have to be proven and once proven they provide the most certain knowledge people have.

Computers and computer science *Computer science is no more about computers than astronomy is about telescopes.* – EDSGER WYBE DIJKSTRA

Computers have changed the way science is practiced in many ways. Data are gathered electronically, scientific papers are composed and distributed electronically, and computational science is arguably a branch of science distinct both from experiment and theory. Familiar programs such as Excel bring into millions of households computational possibilities that were available only at military laboratories 50 years ago, and almost unimaginable 50 years before that.